

الاسم:
الرقم:

مسابقة في الثقافة العلمية: مادة الفيزياء
المدة: ساعة واحدة

This exam is formed of three obligatory exercises in two pages.
The use of non-programmable calculator is recommended.

Exercise 1 (7 ½ pts)

Bouncing of a ball

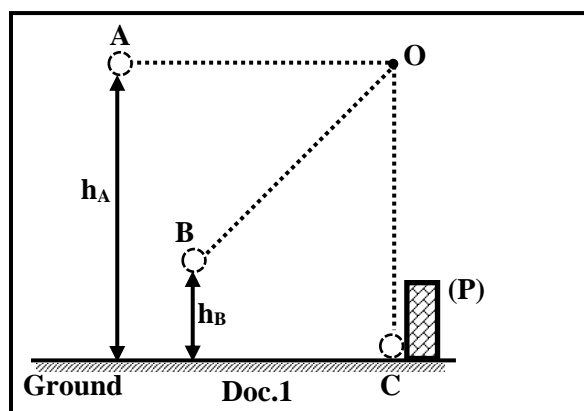
Consider a ball taken as a particle (S) of mass $m = 100 \text{ g}$. (S) is suspended from the lower end of an inextensible massless string, of length 1 m, whose upper end is attached to a fixed point O.

The system [(S) - String] is shifted from its equilibrium position by an angle of 90° , and then (S) is released from rest from point A of height $h_A = 1 \text{ m}$ above the ground. (S) reaches the ground at point C (Doc. 1). Air resistance is neglected during the motion of (S). The aim of this exercise is to study whether (S) is suitable for a certain sports game.

Take:

- the horizontal plane containing C as a reference level for the gravitational potential energy of the system [(S) - Earth];
 - $g = 10 \text{ m/s}^2$.
- 1) Calculate the kinetic energy KE_A of (S) at A.
 - 2) Calculate the gravitational potential energy GPE_A of the system [(S) - String - Earth] at A.
 - 3) Show that the mechanical energy ME_A of the system [(S) - String - Earth] at A is $ME_A = 1 \text{ J}$.
 - 4) The mechanical energy of the system [(S) - String - Earth] is conserved during the motion of (S) from A to C. Why?
 - 5) As (S) reaches the ground at point C, it collides with a plate (P) fixed at the ground. During this collision the system [(S) - String - Earth] loses 55 % of its mechanical energy, and then (S) bounces back and attains a new maximum height h_B .
 - 5.1) Calculate the mechanical energy of the system [(S) - String - Earth] after the collision with the plate (P).
 - 5.2) Deduce that $h_B = 0.45 \text{ m}$.
 - 6) Calculate the ratio $\frac{h_B}{h_A}$.
 - 7) The ball (S) is suitable to be used in a certain sports game if the bouncing ratio is $r = \frac{h_B}{h_A} = 0.54$.

Deduce whether (S) is suitable for this game.



Exercise 2 (6 1/2 pts)

The age of the lunar rocks

The aim of this exercise is to determine the age of the lunar rocks brought back by the Apollo XI astronauts. A sample (A) of this rock is collected. This sample contains certain quantities of the radioactive isotope, potassium-40 (${}^{40}_{19}\text{K}$), as well as the product obtained by its disintegration, argon-40 (${}^{40}_{18}\text{Ar}$).

- 1) Define radioactivity.
- 2) Indicate the composition (number of protons and number of neutrons) of potassium-40.
- 3) One of the decay equations of potassium-40 is: ${}^{40}_{19}\text{K} \rightarrow {}^{40}_{18}\text{Ar} + {}^A_Z\text{X}$.
Calculate Z and A indicating the used laws.
- 4) Indicate the name and the symbol of the emitted particle.
- 5) The half-life (period) of potassium-40 is: $T = 1.25 \times 10^9$ years.

5.1) Define the half-life of a radioactive substance.

5.2) Given that $m_1 = \frac{1}{8} m_0$, where m_1 is the mass of potassium-40 found in the sample (A)

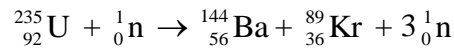
and m_0 is the initial mass of potassium-40 present in the sample (A) when it is formed at $t_0 = 0$.

Determine the age of this sample.

Exercise 3 (6 pts)

Electric energy produced in a nuclear power plant

A nuclear power plant generates electricity from the nuclear energy produced inside its nuclear reactors. Suppose that the nuclear reaction that takes place inside a reactor is:



Given:

Particle or Nucleus	${}^1_0\text{n}$	${}^{235}_{92}\text{U}$	${}^{144}_{56}\text{Ba}$	${}^{89}_{36}\text{Kr}$
Mass in u	1.008	234.994	143.922	88.917

Speed of light in vacuum $c = 3 \times 10^8$ m/s ; $1\text{u} = 1.66 \times 10^{-27}$ kg ; $1\text{MeV} = 1.6 \times 10^{-13}$ J.

- 1) The above nuclear reaction is fission. Justify.
- 2) Show that the loss of mass in this reaction is $\Delta m = 0.139$ u.
- 3) Determine, in joules, the energy E liberated by this reaction.
- 4) Show that the value of this energy in MeV is $E \cong 129.8$ MeV.
- 5) Knowing that 34% of the nuclear energy E is transformed into electrical energy E', calculate E' in MeV.

Exercise 1 (7 ½ pts)

Bouncing of a ball

Part	Answer	Mark
1	$KE_A = \frac{1}{2}mv^2 = 0 \text{ m/s}$	1
2	$GPE_A = mgh_A = 0.1 \times 10 \times 1 = 1 \text{ J}$	1
3	$ME_A = KE_A + GPE_A = 0 + 1 = 1 \text{ J}$	1
4	The air resistance is neglected.	0.5
5	5.1 The remaining mechanical energy just after the collision is: $ME' = 0.45 \times 1 = 0.45 \text{ J}$	1
	5.2 $ME' = KE' + GPE'$ $0.45 = 0 + mgh_B$, $h_B = 0.45 \text{ m}$	1
6	$r = \frac{h_B}{h_A} = r = \frac{0.45}{1} = 0.45$	1
7	No, since $r \neq 0.54$	1

Exercise 2 (6 ½ pts)

The age of the lunar rocks

Part	Answer	Mark
1	The radioactivity is a spontaneous transformation of a nucleus into another one, with emission of radioactive radiation.	1
2	Number of protons $Z = 19$, number of neutrons $N = 21$	0.5
3	According to the law of conservation of mass number : $40 = 40 + A$; $A = 0$ According to the law of conservation of atomic number: $19 = 18 + Z$; $Z = 1$	0.5
	${}_{19}^{40}\text{K} \rightarrow {}_{18}^{40}\text{Ar} + {}_{+1}^0\text{X}$	0.5
4	Name : Positron	0.5
	Symbol : ${}_{+1}^0\text{e}$	0.5
5	5.1 The half-life of a radioactive substance is the time after which half of the radioactive substance is disintegrated.	1
	5.2 $\frac{m_i}{m_f} = 2^n$, $\frac{m_i}{\frac{1}{8}m_i} = 2^n$, $2^3 = 2^n$, $n = 3$ Therefore : $t = nT = 3 \times 1.25 \times 10^9 \text{ years} = 3.75 \times 10^9 \text{ years}$	2

Exercise 3 (6 pts)

Electric energy produced in a nuclear power plant

Part	Answer	Mark
1	This is a provoked nuclear reaction in which a heavy nucleus is divided into two lighter nuclei under the impact of a neutron.	1
2	$\Delta m = m_{\text{before}} - m_{\text{after}} = (234.994 + 1.008) - (143.922 + 88.917 + 3 \times 1.008)$ Then : $\Delta m = 0.139 \text{ u}$	1
3	$E = \Delta m \times c^2$ $\Delta m = 0.139 \times 1.66 \times 10^{-27} = 0.2307 \times 10^{-27} \text{ kg}$ $E = 0.2307 \times 10^{-27} \times (3 \times 10^8)^2 = 2.0766 \times 10^{-11} \text{ J}$	2
4	$E = 2.0766 \times 10^{-11} / 1.6 \times 10^{-13} = 129.79 \text{ MeV} \approx 129.8 \text{ MeV}$	1
5	$E' = 0.34 \times 129.8 \text{ MeV} = 44.132 \text{ MeV}$	1